

**P-1025**

**SET/CSE/SEC/2A2**

**B.C.A./B.Sc. (IT) / B.Sc. (CS)**

**(Fourth Semester)**

**EXAMINATION, 2023-24**

**(Elective Paper)**

**GRAPH PAPER**

*Two Hours ]*

*[ Maximum Marks : 70*

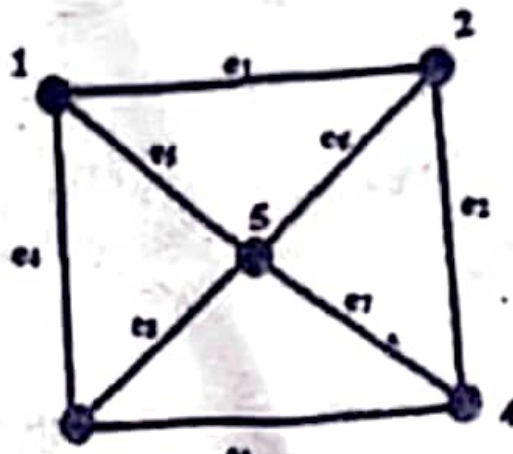
- (i) Attempt any *five* questions (out of seven questions) from Section A and any *three* questions (out of six questions) from Section B.
- (ii) Answer each question of Section A within 50 words.
- (iii) Limit your answers within the given answer book. Additional answer book (B-answer book) should not be provided or used.

**P. T. O.**

## Section—A

**Note :** Attempt any *five* questions. Each question carries 5 marks.

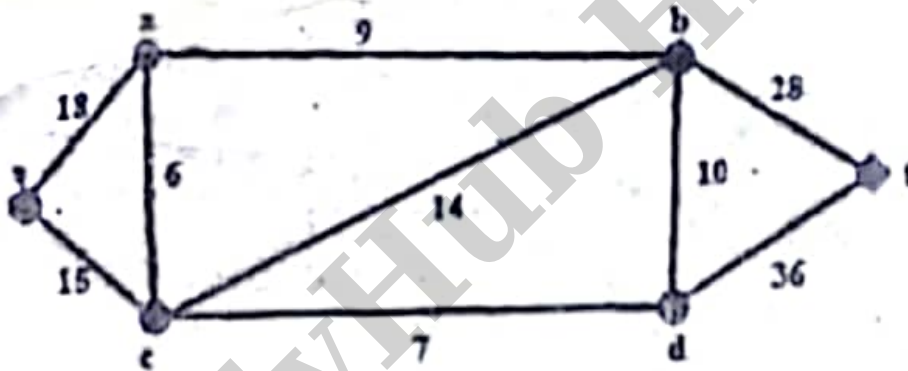
1. What is the maximum number of edges in a simple graph with 7 vertices? Justify your answer.
2. show that all vertices of an Euler graph  $G$  are of even degree.
3. Define walk, path and circuit.
4. Define fundamental circuits and fundamental cut sets.
5. Prove that edge connectivity of a graph cannot exceed the degree of the vertex with the smallest degree in  $G$ .
6. Define chromatic number. What is the chromatic number of a tree with two and more vertices?
7. Construct the adjacency matrix and incidence matrix of the graph.



## Section—B

Note : Attempt any *three* questions. Each question carries 15 marks.

8. Define Eulerian circuit and prove that a connected planar graph with  $n$  vertices and  $e$  edges has  $e-n+2$  regions.
9. Write down Dijkstra's algorithm and use it to find the shortest path from  $s$  to  $t$ .



10. Define Hamiltonian circuits and paths with examples. Find out the number of edge-disjoint Hamiltonian circuits possible in a complete graph with five vertices.
11. Explain connectivity and separability of a graph. What is the maximum vertex connectivity and edge connectivity for the graph shown in the following figure ?